

Assignment-II

- 1) Given,
 loan amount (C) = 20,000 ; Term = 5 years ;
 Monthly installments (X) = 427.90 ; Payment is in arrears.

(i) Then, $20,000 = (12 \times 427.9) a_{\overline{5}|}^{(12)} @ i$

$$\Rightarrow a_{\overline{5}|}^{(12)} = \frac{20,000}{12 \times 427.9} = 3.89499$$

It is known that $APR \sim 2 \times \text{Flat Rate}$.

$$\text{Flat Rate} = \frac{\text{Interest}}{\text{Loan Amount} \times \text{Term}}$$

$$= \frac{-20,000 + 5 \times (12 \times 427.9)}{20,000 \times 5}$$

$$= 5.67\%$$

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$$\therefore APR \sim 11.34\%$$

$$\text{At } APR = 10\% \Rightarrow a_{\overline{5}|}^{(12)} @ i = 10\% = 3.96155$$

$$\text{At } APR = i \Rightarrow a_{\overline{5}|}^{(12)} @ i = 3.89499$$

$$\text{At } APR = 12\% \Rightarrow a_{\overline{5}|}^{(12)} @ i = 12\% = 3.8$$

By linear Interpolation we have $APR = 10.8\%$.

(ii) By prospective method,

$$\text{Capital Outstanding after 1 year} = (12 \times \overset{427.9}{274.49}) a_{\overline{11}|i}^{(12)} @ i = 10.8\% \\ = 16,775.977$$

The outstanding amount of ₹ 16,775.977 is being restructured with new monthly payments (Y) = ₹ 274.49 for t years (say). @ $i = 10.8\%$.

$$\text{Then, } 16,775.977 = (12 \times 274.49) a_{\overline{t}|i}^{(12)} @ i = 10.8\%$$

$$\Rightarrow \frac{1 - (1.108)^{-t}}{12[1.108^{1/12} - 1]} = \frac{16775.977}{12 \times 274.49}$$

$$\Rightarrow (1.108)^{-t} = 0.418205$$

$$\Rightarrow t = \frac{\log(0.418205)}{\log(1.108)}$$

$$\Rightarrow t = 7.25 \text{ years.}$$

Therefore there are 7.25 years left after restructuring the loan.

$$(ii) \text{ Excess Interest} = \text{Total Interest on original loan} - \text{Total interest on restructured loan.}$$

Total interest on original loan is :

$$= 12 \times 4 \times 427.9 - 16775.977$$

$$= 3763.223$$

$$\text{Total interest on restructured loan} = 12 \times 7.25 \times 274.49 - 16775.977$$

$$= 7104.653$$

Therefore Excess interest paid in restructured loan is

$$₹ 7104.653 - ₹ 3763.223 = ₹ 3341.421-$$

3) At 1st November 1985,

$$PV_1 = 200 \times \ddot{a}_{\overline{22}|} @ i=8\% \times (1.08)^{-\frac{3}{12}}$$

$$= 200 \times 10.2007 \times (1.08)^{-\frac{1}{4}}$$

$$= 2161.3633$$

$$PV_2 = 320 \times \ddot{a}_{\overline{16.25}|}^{(4)} @ i=8\% \times (1.08)^{\frac{1}{12}}$$

$$= 320 \times 1.029519 \times \frac{1 - (1.08)^{-16.25}}{0.08} \times (1.08)^{\frac{1}{12}}$$

$$= 2957.8644$$

$$PV_3 = 180 \times \ddot{a}_{\overline{18.75}|}^{(12)} @ i=8\%$$

$$= 180 \times \frac{1 - (1.08)^{-18.75}}{0.08 \left[(1.08)^{\frac{1}{12}} - 1 \right]}$$

$$= 1780.6567$$

4) We know that,

$$(I \ddot{a})_{\overline{n}|} = 1 + 2v + 3v^2 + \dots + nv^{n-1} \quad - \textcircled{1}$$

$$\Rightarrow v(I \ddot{a})_{\overline{n}|} = v + 2v^2 + 3v^3 + \dots + nv^n \quad - \textcircled{2}$$

$\textcircled{1} - \textcircled{2}$, we have,

$$\Rightarrow (1-v)(I \ddot{a})_{\overline{n}|} = 1 + v + v^2 + v^3 + \dots + v^{n-1} - nv^n$$

$$\Rightarrow (1-v)(I \ddot{a})_{\overline{n}|} = \ddot{a}_{\overline{n}|} - nv^n$$

$$\Rightarrow (I \ddot{a})_{\overline{n}|} = \frac{\ddot{a}_{\overline{n}|} - nv^n}{d}$$

5) (i) Time - Weighted rate of Return for Property Fund

$$TWRR = \frac{16.4}{12.4} - 1 = 32.258\%$$

Time - Weighted rate of Return for Equity Fund

$$TWRR = \frac{15.5}{12.1} - 1 = 28.099\%$$

(ii)

b)

$$(i) \text{ Initial amount of Capital Repayment} = \frac{160,000}{a_{\overline{10}|i=8\%}}$$

$$= \frac{160000}{6.7101}$$

$$= 23844.652$$

(ii) After 4th repayment, the capital outstanding is

$$= 23844.652 a_{\overline{6}|i=8\%}$$

$$= 23844.652 \times 4.6229$$

$$= 110231.4422$$

But now i changed from 8% to 10%. So,

$$\text{New repayment amount} = \frac{110231.4422}{a_{\overline{6}|i=10\%}}$$

$$= \frac{110231.4422}{4.3553}$$

$$= 25,309.72428$$

$$(ii) \text{ Capital outstanding after 7th repayment} = 25309.72428 \times a_{\overline{3}|10\%}$$

$$= 25309.72428 \times 2.4869$$

$$= 62942.75331$$

Now, 'i' changed from 10% to 9% so new repayment amount = $\frac{62942.75331}{a_{\overline{3}|9\%}}$ @ i=9%

$$= \frac{62942.75331}{2.5313} = 24865.78174$$

7) (i) Reasons:-

- a) Property is less liquid than government security
- b) Investing in Govt. security provides guaranteed coupon payment.
- c) There are extra expenses incurred after purchasing property.

(ii)

c)

1) Debentures:-

The investor may not receive income if the company does not pay interest.

2) Equity Shares:-

The investor will not have a guarantee of certain income as dividends change with respect to dividend policy of a company.

3) Property:-

It is related to availability of demand for property rentals.

9)

(i) TWRR :-

$$(1+i)^3 = \frac{33}{30.5} \times \frac{41.05 - 4.5}{33 + 6} \times \frac{45.6}{41.05} \times \frac{47}{45.6 - 2.5}$$

$$\Rightarrow (1+i)^3 = 1.2283132$$

$$\Rightarrow i = 7.095\%$$

MWRR :-

$$47 = 30.5(1+i)^3 + 6(1+i)^{2.25} + 4.5(1+i)^{1.5} - 2.5(1+i)^{0.5}$$

$$\text{At } i = 7\%, \quad AV = 46.745$$

$$i = 8\%, \quad AV = 48.008$$

By linear interpolation, we have, $MWRR = i = 7.2\%$

(ii)

(ii) linked rate of return:-

$$(1+i)^3 = \left[1 + \left(\frac{38.5 - 30.5}{30.5} \right) \right] \times \left[1 + \left(\frac{45 - 38.5}{38.5} \right) \right] \times \left[1 + \left(\frac{47 - 45}{45} \right) \right]$$

$$\Rightarrow (1+i)^3 = 1.5409836$$

$$\Rightarrow i = \text{LIRR} = 15.504\%$$

(10) Given,

(i)

First Installment = ₹ 2,00,000/- = P (say)

Installment in subsequent years = ₹ 20,000/- = Q (say).

Then, let the approved loan amount = X.

Then,

$$PV = (P-Q) a_{\overline{n}|i} + Q (Ia)_{\overline{n}|i}$$

$$\Rightarrow X = 180000 a_{\overline{15}|12\%} + 20,000 (Ia)_{\overline{15}|12\%}$$

$$\Rightarrow X = ₹ 20,40,582.$$

$$\text{Then, Total Cost of the house} = \frac{20,40,582}{80\%} = ₹ 25,50,727.5/-$$

(ii) Loan Schedule :-

Year	Loan O/S at beginning	Repayment Installment	Interest Paid	Capital Repaid	Loan O/S at end
9	18,75,852	3,60,000		13,48,97.76	17,40,954.24
			2,25,12.24		
10	17,40,954.24	3,80,000		17,10,85.49	15,69,868.75
			2,08,914.51		

Working notes :-

At year 9 :-

$$\text{Installment amount} = 2,00,000 + (9-1)(20,000) = 3,60,000$$

$$\begin{aligned} \text{Loan O/S at beginning} &= PV_{t=8} = 3,40,000 a_{\overline{7}|12\%} + 20,000 (Ia)_{\overline{7}|12\%} \\ &= 18,75,852 \end{aligned}$$

At year 10 :-

$$\text{Installment amount} = 3,60,000 + 20,000 = 3,80,000$$

$$\begin{aligned} \text{Loan O/S at beginning} &= - (18,75,852 \times 12\%) + 3,60,000 \\ &= 18,75,852 - (3,60,000 - (18,75,852 \times 12\%)) \\ &= 17,40,954.24 \end{aligned}$$

~~(1P)~~

(1)

(i) let X be the value of fund on 31/12/16.

Then,

$$(1.20)^2 = \frac{500}{460} \times \frac{550}{500} \times \frac{600}{550} \times \frac{X}{600}$$

$$\Rightarrow X = 662.4$$

(ii) MWRR:-

$$662.4 = 460(1+i)^2 + 40(1+i)^{\frac{21}{24}} - 50(1+i)$$

$$\Rightarrow i = 21.19\%$$

(iii) Linked rate of return:-

$$(1+i)^2 = \left(1 + \frac{550-460}{460}\right) \left(1 + \frac{662.4-550}{550}\right)$$

$$\Rightarrow (1+i)^2 = 1.44 \Rightarrow i = 20\%$$

$$LIRR = 20\%$$

13)

(i) Let monthly repayment be X .

$$\text{Then, } 9,88,000 = 12X a_{\overline{25}|}^{(12)} @ i = 7\%$$

$$\Rightarrow = 12X \left(\frac{1 - (1.07)^{-25}}{12[(1.07)^{1/12} - 1]} \right)$$

$$\Rightarrow X = 82176.89243 \times \frac{1}{12}$$

$$= 6848.07437$$

(ii) Let the required loan A/S amount be X . Then,

$$X = 6848.07437 a_{\overline{136}|}^{(12)} @ \frac{i}{12}$$

$$\Rightarrow X = 6,48,577.7278$$

$$(iii) \text{ PV at } 10/09/2026 = 6848.07437 a_{\overline{166}|}^{(12)} @ \frac{i}{12}$$

$$= 7,36,123.4837$$

$$\text{PV at } 10/10/2026 = 6848.07437 a_{\overline{165}|}^{(12)} @ \frac{i}{12}$$

$$= 7,33,437.5845$$

$$\text{Capital repaid} = 736123.4837 - 733437.5845 = ₹ 2685.909224$$